| MATRICULATION AND SECONDARY EDUCATION CERTIFICATE EXAMINATIONS BOARD UNIVERSITY OF MALTA, MSIDA <br> SECONDARY EDUCATION CERTIFICATE LEVEL SEPTEMBER 2013 SESSION |  |
| :---: | :---: |
| SUBJECT: Mathematics PAPER: I- Section A (Non-C <br> DATE: $2^{\text {nd }}$ September 2013 TIME: 20 minutes | culator Section) |
| ATTEMPT ALL QUESTIONS. <br> Write your answers in the space available on the examination paper. The use of calculators and protractors is NOT allowed. <br> It is not necessary to show your working. <br> This paper carries a total of 20 marks. |  |
| Questions And Answers <br> All Questions Carry One Mark | Space For Rough Work (If Necessary) |
| 1 Work out $\frac{2^{3} \times 54}{3^{2} \times 16}$. |  |
| 2 Write down the sum of the next two numbers in the sequence: $13,9,5,1,$ $\qquad$ , _. $\qquad$ |  |
| 3 Change 2.72 to an improper fraction in its lowest terms. |  |


| Questions And Answers <br> All Questions Carry One Mark | Space For Rough Work (If Necessary) |
| :---: | :---: |
| 4 How much is $150 \%$ of $€ 200$ ? |  |
| 5 Express 0.6725 litres in mls. |  |
| 6 A sum of money is divided between Peter and Paul in the ratio of 7: 13. If Paul gets $€ 60$ more than Peter, what was the sum of money? <br> Ans |  |
| 7 There are 20 pink pages, 15 green pages and 25 yellow pages in a book. I open the book at random and choose a page. What is the probability that I land on a green page? <br> Ans |  |
| 8 The area of triangle $X Y Z$ is $25 \mathrm{~cm}^{2}$. If the altitude $X P$ is 4 cm , find the length of YZ. |  |
| 9 Find the gradient of a line parallel to the line with equation $2 y=6 x-17$. |  |
|  |  |

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| Questions And Answers <br> All Questions Carry One Mark | Space For Rough Work (If Necessary) |
| :---: | :---: |
| 10 Find the area of rectangle $A B C D$, given that the diagonal $A C$ is of length 5 m and side CD is 3 m long. |  |
| 11 The price of an object increased from $€ 20$ to $€ 23$. What is the percentage increase? |  |
| 12 Give an estimate of $\frac{201^{2}}{96(\pi)}$, correct to two significant figures. <br> Ans |  |
| 13 The mean of four numbers is 13 . Three of the numbers are 7,12 and 14 . What is the fourth number? <br> Ans |  |
| 14 Lara goes to sleep at $21: 45$ on Sunday. At what time does she wake up on Monday if she sleeps exactly 8 hours and 20 minutes? |  |
| Ans |  |

$\qquad$

| Questions And Answers <br> All Questions Carry One Mark | Space For Rough Work (If Necessary) |
| :---: | :---: |
| 15 If a circle with radius $r$ has an area of $100 \mathrm{~cm}^{2}$, what is the area of a circle with radius $2 r$ ? |  |
| 16 Work out $\frac{1}{2}+\frac{1}{3}-1$. |  |
| 17 Find the value of $x^{2}-x y$ when $x=502$ and $y=2$. $\qquad$ Ans |  |
| 18 Find the negative value of $x$ that satisfies the equation: $2 x^{2}=12800$ <br> Ans |  |
| 19 The cost of theatre tickets for 10 adults and 4 children is $€ 152$, while the cost of the same tickets for 4 adults and 10 children is $€ 128$. What is the cost of the theatre tickets for 1 adult and 1 child? |  |
| 20 The edges of a closed box are to be sealed with glue. Find the total length of the edges to be sealed, if the box has sides 10 cm , 5 cm and 6 cm . <br> Ans |  |

## MATRICULATION AND SECONDARY EDUCATION CERTIFICATE EXAMINATIONS BOARD UNIVERSITY OF MALTA, MSIDA

## SECONDARY EDUCATION CERTIFICATE LEVEL

## September 2013 SESSION

| SUBJECT: | Mathematics |
| :--- | :--- |
| PAPER NUMBER: | I - Section B (Calculator Section) |
| DATE: | $2^{\text {nd }}$ September 2013 |
| TIME: | 1 hr and 40 minutes |

## ANSWER ALL QUESTIONS

Write your answers in the space available on the examination paper.
Show clearly all the necessary steps, explanations and construction lines in your working.
Unless otherwise stated, diagrams are drawn to scale.
The use of non-programmable electronic calculators with statistical functions and mathematical instruments is allowed.

Candidates are allowed to use transparencies for drawing transformations.
This paper carries a total of 80 marks.


1 (a) When water freezes, its volume increases by $4 \%$. What volume of water is needed to make $468 \mathrm{~cm}^{3}$ of ice?

3 marks
(b) Find the value of $x$ such that $3^{2 x+1}=81$

2 The value $\boldsymbol{R}$ can be calculated from $\boldsymbol{P}$ and $\boldsymbol{Q}$, using the formula:

$$
\frac{1}{R}=\frac{1}{P}+\frac{1}{Q}
$$

(i) Given that $\boldsymbol{P}=150$ and $\boldsymbol{Q}=250$, calculate the value of $\boldsymbol{R}$.
(ii) Find $\boldsymbol{P}$ in terms of $\boldsymbol{R}$ and $\boldsymbol{Q}$.

3 Gary sells two kinds of books, hardbacks and paperbacks. The income from selling 15 hardbacks and 28 paperbacks is $€ 779$. When he sells 9 hardbacks and 16 paperbacks his income is $€ 455$.
(i) Let $h$ represent the price of a hardback and let $p$ represent the price of a paperback. Write down two equations to show the given data.

## 4 marks

(ii) Solve the two simultaneous equations to find the price of each kind of book.

## 5 marks

4 A wax candle is in the shape of a cylinder of radius 4 cm and height 6 cm .
(i) Find the volume of the wax cylinder. Give your answer in $\mathrm{cm}^{3}$, correct to 2 decimal places.

## 3 marks

(ii) The wax cylinder is melted to form a cube, but $4 \%$ of the wax is lost in the process. Calculate the side of the cube formed from the wax, giving your answer in cm , correct to 2 decimal places.

5 I use two digits from 1 to 5 to form a number.
(i) Draw a possibility space to show all the possible 2-digit numbers I can form.
(ii) What is the probability that the two digits in the number add up to 7 ?
(iii) What is the probability that the number formed is a multiple of 4 ?

6 The following figure consists of a trapezium ABCD , a rectangle CDFG and an isosceles triangle FEG, right-angled at E.


The diagram is not drawn to scale
(i) If $\mathrm{FG}=5.2 \mathrm{~m}$, calculate the length of sides FE and EG of triangle GEF in m, correct to 3 significant figures.

## 3 marks

(ii) Given also that the height of the trapezium is $6.5 \mathrm{~m}, \mathrm{AB}=2.5 \mathrm{~m}$ and $\mathrm{GC}=1.3 \mathrm{~m}$, work out the total area of the figure, giving your answer in $\mathrm{m}^{2}$, correct to 3 significant figures.

## 6 marks

7 The prices in a shop selling household appliances were all raised by $5 \%$ at the beginning of this year.
(i) Find the price of a washing machine which cost $€ 355$ last year.

## 2 marks

(ii) How much would I have paid for a microwave oven, now marked $€ 103.95$, had I bought it last year?

## 3 marks

(iii) A sale is announced at the shop for the Christmas season offering a discount. How much would the percentage discount have to be so that the prices return to those of last year? Give your answer correct to 2 decimal places.

8 (i) The cost of Platinum is quoted in dollars at $\$ 1,687.80$ per kg and that of Silver in Euro at $€ 23.722$ per kg. If $\$ 1=€ 0.7416$, find the ratio of the price of Platinum to that of Silver. Give your answer in the form $r: 1$ where $r$ is correct to 2 decimal places.

## 3 marks

(ii) The price of Gold is quoted as $€ 38.75$ per troy ounce. If 1 g equals 0.03215 troy ounces, find the ratio of the price of Gold to that of Silver. Give your answer in the form $r: 1$ where $r$ is correct to 2 decimal places.

## 9 Use ruler and compasses only to:

(i) construct triangle ABC with $\mathrm{AB}=6 \mathrm{~cm}, \mathrm{AC}=11 \mathrm{~cm}$ and $\mathrm{BC}=7 \mathrm{~cm}$;
(ii) drop a perpendicular CD from C to AB produced;
(iii) bisect angle BAC and let this bisector cut CD at E ;
(iv) measure ED.
(v) Use a protractor to measure angle CBD.

10 The diagram below shows a circle with centre $O$ and tangent $A B$. The circle has radius 9 cm and $A B$ is 12 cm long.

The diagram is not drawn to scale.

(i) Calculate the length of AO.
(ii) Find angle BOA to the nearest degree.
(iii) Find angle BCO to the nearest degree.
(iv) If M is the midpoint of BC , explain why OM is perpendicular to BC .
(v) Calculate the length of the chord BC in cm , correct to 1 decimal place.

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## MATRICULATION AND SECONDARY EDUCATION CERTIFICATE EXAMINATIONS BOARD UNIVERSITY OF MALTA, MSIDA

## SECONDARY EDUCATION CERTIFICATE LEVEL

## SEPTEMBER 2013 SESSION

| SUBJECT: | Mathematics |
| :--- | :--- |
| PAPER NUMBER: | IIB |
| DATE: | $2^{\text {nd }}$ September 2013 |
| TIME: | $4: 00$ p.m. to 6:00 p.m. |

## ANSWER ALL QUESTIONS

Write your answers in the space available on the examination paper.
Show clearly all the necessary steps, explanations and construction lines in your working.
Unless otherwise stated, diagrams are drawn to scale.
The use of non-programmable electronic calculators with statistical functions and mathematical instruments is allowed.

Candidates are allowed to use transparencies for drawing transformations.
This paper carries a total of 100 marks.

| For Office Use Only |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
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| Question No | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |  |  |  |  |  |
| Mark |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |


| Question No | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Mark |  |  |  |  |  |  |  |  |  |  |

1 Write down $2.65731 \times 10^{4}$ as an ordinary number to 3 significant figures.

2 Find the product of the sum and the difference of the numbers 23 and 173.

## 3 marks

3 Find the Least Common Multiple (LCM) of the numbers 121, 220 and 880.

## 3marks

4 One kilowatt-hour unit of electricity is consumed when an appliance of 1000 W is used for one hour. How many kilowatt-hour units of electricity are consumed when a vacuum cleaner, having power of 900 W , is used for 20 minutes?

## 2 marks

5 Simplify: $\frac{b^{-2}}{a^{5}}\left(\frac{a^{2}}{b}\right)^{3} \frac{1}{(a b)^{-1}}$

2 marks

6 (i) Write down 3 prime numbers between 20 and 40 .
(ii) What is the smallest number that must be added to 220 to get a perfect square?

1 mark

7 A club organises a lottery, selling tickets at 25 c each. What is the least number of tickets that must be sold, if the prize cost the club $€ 58$ and the club aims to make a profit of $€ 150$ ?

8 Using a calculator, work out $3 \sin 60^{\circ} \times \sqrt{\frac{45}{\cos 30^{\circ}}}$ correct to 2 decimal places.

2 marks

9 The first 4 terms of a sequence are: 22, 17, 12, 7, ...
(i) Write down the next 2 terms in the sequence.
(ii) Write down a formula for the $n^{\text {th }}$ term of this sequence.

10 Solve the equation $x(x+9)=x^{2}-3 x+48$

## 3 marks

11 Use the formula $c^{2}=b^{2}+2 a s$ :
(i) to calculate the two values of $c$ when $b=-2, a=9.8$ and $s=12$, correct to 3 significant figures;
(ii) to find an expression for $s$ in terms of $a, b$ and $c$.

12 In the figure below, ABC is a triangle, with sides $\mathrm{AB}, \mathrm{AC}$ and BC produced as shown. The angle marked $a$ is $82^{\circ}$ and the angle marked $b$ is $28^{\circ}$.

(i) Write down the size of angle ACB , giving a reason for your answer.
(ii) Find angle CAB.

2 marks

13 Sara wakes up at 06:25 to prepare for work. She usually leaves home at 07:20 and drives to work for 28 minutes.
(i) Calculate the time at which Sara arrives at work.

1 mark
(ii) Find the time Sara takes from when she wakes up, to when she leaves home.
(iii) One day, Sara wants to arrive at work at $07: 45$, but decides to walk, taking 39 minutes. What is the latest time at which Sara should wake up, if she takes the usual time to prepare for work?

14 The picture shows the scale on a thermometer. On the left side the scale is graduated in degrees Fahrenheit and on the right side in degrees Celsius.
(i) Write down the temperature reading shown in degrees Celsius.
(ii) Degrees Celsius ( $C$ ) can be changed to degrees Fahrenheit $(F)$ by the formula $F=\frac{9}{5} C+32$. Change a temperature of $50^{\circ} \mathrm{C}$ to degrees Fahrenheit.
(iii) Calculate the temperature below freezing point, at which the temperature readings are the same in both degrees Celsius and degrees Fahrenheit.

15 An arc PQ of length 15 cm subtends an angle of $60^{\circ}$ at the centre O of a circle.

(i) Calculate the radius of the circle, leaving your answer in terms of $\pi$.
(ii) Prove that the chord PQ is equal to the radius of the circle.

16 A college has 250 students. The number of days that students were absent in a particular period of 15 school days was recorded as follows:

| Days absent | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No. of students | 18 | 11 | 12 | 8 | 15 | 20 | 19 | 16 | 17 | 13 | 15 | 11 | 8 | 5 | 4 |

(i) How many students were never absent during that period?
(ii) Write down the mode.
(iii) What percentage of students were absent for more than 10 days?
(iv) Taking all the students at the college, what is the mean number of absent days per student, correct to 1 decimal place?

17 ABCD is a quadrilateral inscribed in a circle. BA is produced to E . Angle $\mathrm{DAE}=80^{\circ}$ and angle $\mathrm{CBD}=50^{\circ}$.


The diagram is not drawn to scale.
(i) Find angle DCB, explaining your reasoning.
(ii) Prove that $\mathrm{CD}=\mathrm{CB}$.

18 Consider the equation $4 y=x+8$.
(i) Find the value of $x$ when $y=0$.

1 mark
(ii) Fill in the table given below, for values of $x$ between -5 and 3 , in the given equation.

| $x$ | -5 | -4 | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $y$ |  |  |  |  |  |  |  |  |  |

3 marks
(iii) On the diagram below, you are given the graph of the line with equation $y=x+5$. Using the same set of axes, draw the graph of $y$ against $x$ for the table obtained in (ii).


3 marks
(iv) Use your graph to find the value of $y$ at which $x=\frac{x+8}{4}-5$.

19 George can cycle at 15 km per hour and walk at 7 km per hour. One morning he starts on a journey, cycling a distance of 8 km and then proceeding on foot for 45 minutes.
(i) Express his cycling speed in $\mathrm{m} / \mathrm{s}$ correct to 3 decimal places.
(ii) Find the time that George spent cycling.
(iii) Find the total distance covered by George.
(iv) Calculate the average speed over the whole journey, giving your answer in $\mathrm{km} / \mathrm{hour}$, correct to 2 decimal places.

20 The diagram shows a river running parallel to a block of flats. The height of the block is 32 m . Looking down from the roof from a point P directly across the river, the angle of depression of the nearer bank A is $53^{\circ}$ and that of the further bank B is $34^{\circ}$.

(i) How far is the block from the nearer river bank A? Give your answer in metres, correct to 2 decimal places.
(ii) Calculate the width of the river in metres, correct to 2 decimal places.
(iii) Calculate how far P is from the river bank B , in metres, correct to 2 decimal places.

